Effect of pressure on the magnetic properties of CrB₂

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The magnetic susceptibility χ of the itinerant antiferromagnet CrB_2 with $T_N \approx 87$ K is studied as a function of the hydrostatic pressure up to 2 kbar at fixed temperatures 78 and 300 K. The pressure effect on χ is found to be negative in sign and weakly dependent on the magnetic state of the compound. In addition, the measured pressure dependence of the Néel temperature, dT_N/dP =0.1±0.1 K/kbar, is roughly two orders of magnitude smaller than the corresponding value for the pure chromium. The main contributions to χ and their volume dependence are calculated *ab initio* within the local spin density approximation, and they turn out to be in close agreement with the experimental data. © 2009 American Institute of Physics. [DOI: 10.1063/1.3168639]

I. INTRODUCTION

CrB2 is an itinerant-electron antiferromagnet with Néel temperature $T_N = 85 - 88$ K,¹⁻⁴ possessing a hexagonal crystal structure of the $\ensuremath{AlB_2}$ type. As follows from a neutron diffraction study on the single crystal, CrB₂ has a complicated helicoidal magnetic structure, and the magnetic moment (of about $0.5\mu_B$ per Cr atom at T=0) turns in the *ac* plane.⁵ The electronic specific heat of CrB₂, $\gamma = 13.6 \text{ mJ}/(\text{K}^2 \cdot \text{mol})$,³ is abnormally high in comparison with those of the nonmagnetic 3d-metal diborides such as ScB₂, TiB₂, and VB₂ $(1-5 \text{ mJ}/(\text{K}^2 \cdot \text{mol}))$.^{2,3,6} The electronic spin susceptibility of CrB₂ is also an order of magnitude higher than that of other diborides, demonstrating a large exchange-enhancement effect. The band structure calculations for CrB₂ (Refs. 7-10) have shown that its Fermi level lies in a region of the high density of electronic states (DOS). Therefore the Stoner criterion is nearly fulfilled in CrB₂, and the susceptibility enhancement factor, $S \simeq 9$, was estimated.^{7,9} In addition, the spin density wave (SDW) along the hexagonal axis was predicted in Ref. 7 to be due to the nesting of the 7th-band Fermi surface. However, both the predicted SDW type of magnetic structure and the estimated magnetization of σ $\simeq 0.01 \mu_B$ per Cr atom are inconsistent with the experimental neutron data.⁵ It should be noted that more reasonable value of magnetization, $\sigma \simeq 0.3 \mu_B$ per Cr atom, was obtained in the recent spin-polarized band structure calculations for CrB2.10

Here we report results of our investigations of the pressure effect on the magnetic susceptibility and Néel temperature of CrB_2 compound to clarify the nature of its magnetic properties and details of the antiferromagnetic (AFM) transition. The experimental data are supplemented by *ab initio* calculations of the volume dependent band structure and magnetic susceptibility.

II. EXPERIMENTAL DETAILS AND RESULTS

The polycrystalline sample of CrB_2 compound was initially prepared by arc-melting of the stoichiometric amount of Cr and B elements of better than 99.8% purity in a water cooled crucible under a protective argon atmosphere. The ingot was then crushed to powder and pressurized. The pressed sample was sintered at $T \approx 1500 \,^{\circ}\text{C}$ followed by its melting in an induction furnace and annealing. The study of x-ray powder diffraction at room temperature revealed that sample has the AlB₂-type hexagonal crystal structure, and the obtained lattice parameters agree closely with that published in literature.¹¹ No other phases were detected within the resolution of the employed x-ray technique.

For additional examination of the sample quality, its magnetic susceptibility was measured as a function of temperature for the magnetic field H=0.8 T using the Faraday microbalance method. The data obtained show a clear peak at $T \approx 87$ K (see Fig. 1), which corresponds to magnetic ordering in the system. The observed $\chi(T)$ behavior is in agreement with the known data in the literature for high-quality CrB₂ samples.⁴

The pressure effect on the magnetic susceptibility was measured under helium gas pressure up to 2 kbar at two fixed temperatures, 78 and 300 K, using a pendulum-type magnetometer placed into the nonmagnetic pressure cell.¹² The relative errors of our measurements, performed in the magnetic field H=1.7 T, did not exceed 0.05%. The experimental pressure dependencies of the magnetic susceptibility of CrB₂ are shown in Fig. 2, which demonstrate a magnitude of the pressure effect and its linear behavior. For each temperature the values of χ at ambient pressure and their pressure derivatives $d \ln \chi/dP$ are listed in Table I. In order to transform the pressure derivative into the volume derivative,

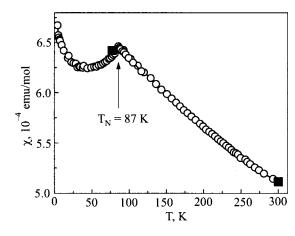


FIG. 1. Temperature dependence of the magnetic susceptibility for CrB_2 . The data obtained with a pendulum magnetometer at P=0 are presented by filled squares.

we used the calculated bulk modulus value (B=2.3 Mbar, see Sec. III A).

With the aim of finding the pressure effect on the Néel temperature, the $\chi(T)$ dependence was studied in detail around T_N for two different pressures (see Fig. 3). The resulting pressure derivative $dT_N/dP=0.1\pm0.1$ K/kbar was estimated from the shift of the maximum in $\chi(T)$ and appears to show only weak tendency for T_N to increase with pressure.

III. COMPUTATIONAL METHOD AND RESULTS

A. Band structure calculations

The investigated diboride CrB_2 possesses the hexagonal AlB₂ (*C*32) crystal structure which is composed of transition-metal layers alternating with graphite-like boron layers stacked perpendicularly to the [001] axis. *Ab initio* calculations of the electronic structure of CrB_2 were carried out by employing a modified FP-LMTO method.¹³⁻¹⁵ The exchange-correlation potential was treated in the local density approximation (LDA)¹⁶ of the density functional theory.

The calculated density of states N(E) for the paramagnetic (PM) phase of CrB₂ is shown in Fig. 4, and it is in qualitative agreement with the results of KKR-ASA⁷ and LMTO-ASA⁸⁻¹⁰ calculations. The calculated DOS at the

TABLE I. The magnetic susceptibility of CrB_2 (in 10^{-4} e.m.u./mol) and its pressure (in Mbar⁻¹) and volume derivatives at different temperatures.

Т, К	χ		$d \ln \chi/dP$	d ln χ/d	In V
	exp.	theor. ^a	exp.	exp.	theor. ^a
0	7.3 ^b	7.5	-	-	4.0
78	6.42	-	-1.82 ± 0.3	-4.2 ± 0.7	-
300	5.11		-1.65 ± 0.2	-3.8 ± 0.5	-

^afor the paramagnetic state;

^bextrapolation of the experimental data for the paramagnetic state in Fig. 1.

Fermi level $N(E_F)$ =31.7 Ry⁻¹ is comparable with the results of LMTO-ASA calculations, 33.7 Ry⁻¹ (Ref. 8) and 34.9 Ry⁻¹ (Ref. 10), but differs substantialy from the earlier result of non-self-consistent calculations of Ref. 7, $N(E_F)$ =20.9 Ry⁻¹. As is seen from Fig. 4, in CrB₂ the Fermi level is located at the steep slope of the N(E) peak, where the DOS increases rapidly with energy. Among other 3*d* diborides, CrB₂ possesses a comparatively large value of $N(E_F)$, resulting in a strongly enhanced spin paramagnetism of the compound and transition to the magnetically ordered state at *T* =87 K.

To calculate the bulk modulus value to be used in the analysis of pressure effects in CrB₂, band structure calculations were performed for a number of lattice parameters close to the experimental ones (the ratio c/a was fixed at its experimental value 1.033). The equilibrium unit cell volume $V_{\rm th}$ and the corresponding theoretical bulk modulus B_{LDA} were determined from the calculated volume dependence of the total energy E(V) by using the well known Murnaghan equation,¹⁴ and turn out to be $V_{\text{th}}=21.79$ Å³ and B_{LDA} =3.23 Mbar. The Murnaghan equation is based on the assumption that the pressure derivative B' of the bulk modulus B is constant. Using the value B' = 3.9 found from the Murnaghan equation, we have estimated $B \simeq 2.3$ Mbar, corresponding to the *experimental* volume V_{exp} =23.41 Å³ (Ref. 17). This correction counterbalances the well-known overbonding tendency of the LDA approach¹⁴ and provides better agreement with the experimental values of the bulk moduli,

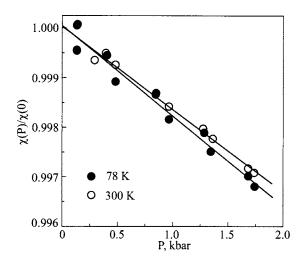


FIG. 2. Pressure dependence of the magnetic susceptibility for CrB_2 at *T* = 78 and 300 K, normalized to its value at *P*=0.

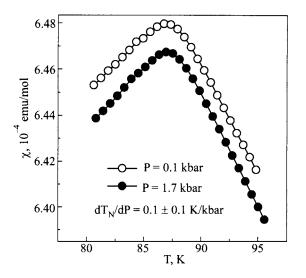


FIG. 3. Temperature dependence of the magnetic susceptibility for CrB_2 in the vicinity of T_N at two fixed pressures.

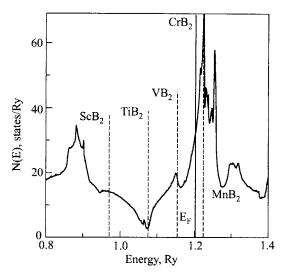


FIG. 4. Density of states for CrB_2 . The vertical lines indicate the conduction band filling for the corresponding 3*d* diborides.

as follows from our previous calculations.^{13,15}

B. Magnetic susceptibility

The FP-LMTO calculations of the field-induced spin and orbital (Van Vleck) magnetic moments were carried out selfconsistently within the procedure described in Refs. 13 and 15 by means of the Zeeman operator,

$$\hat{H}_Z = \mathbf{H} \cdot (2\hat{\mathbf{s}} + \hat{\mathbf{l}}),\tag{1}$$

which was incorporated in the original FP-LMTO Hamiltonian. Here **H** is the external magnetic field, \hat{s} and \hat{l} are the spin and orbital angular momentum operators, respectively. The field-induced spin and orbital magnetic moments were calculated in an external field of 10 T and provided estimation of the related contributions to the magnetic susceptibility, $\chi_{\rm spin}$ and $\chi_{\rm orb}$. For the hexagonal C32 crystal structure of CrB_2 , the components of these contributions, $\chi_{i\parallel}$ and $\chi_{i\perp}$, were derived from the magnetic moments obtained in an external field, applied parallel and perpendicular to the caxis, respectively. The averaged values of the calculated $\chi_{\rm spin}$ and χ_{orb} components, $\chi_i = (\chi_{i\parallel} + 2\chi_{i\perp})/3$, and the evaluated magnetic anisotropy, which is determined by the orbital contribution, $\Delta \chi_{\text{orb}\parallel} = \chi_{\text{orb}\parallel} - \chi_{\text{orb}\perp}$, are listed in Table II. For completeness, the table also contains an estimate of the Langevin diamagnetism of filled shells χ_{dia} , which turns out to be close to a free-ionic diamagnetic susceptibility.^{18,19}

In addition, the enhanced Pauli spin contribution to the magnetic susceptibility was also calculated within the Stoner model:

TABLE II. Calculated bulk modulus B and contributions to the magnetic susceptibility of CrB_2 in the PM state (see text for details).

<i>B</i> , Mbar	Xston	xspin	χorb	Δχ _{orb}	Xdia	χ ^a sum			
	10 ⁻⁴ emu/mol								
2.30	4.0	7.03	0.60	0.010	-0.10	7.53			
$\chi_{\rm sum}^{\alpha} = \overline{\chi}_{\rm spin} + \overline{\chi}_{\rm orb} + \chi_{\rm dia}.$									

$$\chi_{\text{ston}} = S\chi_P \equiv \mu_B^2 N(E_F) [1 - IN(E_F)]^{-1},$$
 (2)

where $\chi_P = \mu_B^2 N(E_F)$, *S* is the Stoner enhancement factor, and μ_B is the Bohr magneton. The Stoner integral *I*, describing the exchange-correlation interaction of the conduction electrons, can be expressed in terms of the calculated parameters of the electronic structure:^{20,21}

$$I = \frac{1}{N(E_F)^2} \sum_{qll'} N_{ql}(E_F) J_{qll'} N_{ql'}(E_F).$$
(3)

Here $N(E_F)$ is the total density of electronic states at the Fermi level E_F , $N_{ql}(E_F)$ is the partial density of states for atom q in the unit cell, $J_{qll'}$ are the local exchange integrals:

$$J_{ll'} = \int g(\rho(r))\phi_l(r^2)\phi_{l'}(r)^2 dr,$$
(4)

where $\phi_l(r)$ are the partial wave functions, and $g(\rho(r))$ is a function of the charge density.¹⁶ The calculated value of the enhanced Pauli susceptibility χ_{ston} is presented in Table II and turns out to be lower than the field-induced spin susceptibility χ_{spin} , evaluated by using the full Zeeman term (1). It should be noted, that the field-induced and Pauli spin susceptibilities in Table II were calculated for the equilibrium unit cell volume V_{th} .

IV. DISCUSSION

In CrB₂ the main contribution to $N(E_F)$ comes from dstates of Cr, and the Stoner criterion is nearly fulfilled due to the large value of $N(E_F)$ (see Fig. 4). The calculated susceptibility enhancement factor $S=[1-IN(E_F)]^{-1}$ turns out to be about 8, which is comparable with earlier estimates $(S \approx 9)$.⁷ In the PM phase of CrB₂ the magnetic susceptibility rises with decreasing temperature and reaches a value $\chi_{exp} \approx 6.5 \times 10^{-4}$ e.m.u/mol at T=90 K. The extrapolated PM susceptibility $\chi_{exp}(T \rightarrow 0)$ provides the estimate $\chi_{exp}(0) \approx 7.3 \times 10^{-4}$ e.m.u/mol, which is in agreement with the calculated paramagnetic contributions χ_{spin} and χ_{orb} from Table II. The calculated small value of the magnetic anisotropy in CrB₂ (less than 1%) is also in line with the experimental data of Ref. 4.

The total susceptibility of metallic systems in the absence of spontaneous magnetic moment can be expressed as the sum^{15,19}

$$\chi_{\text{tot}} = \chi_{\text{spin}} + \chi_{\text{orb}} + \chi_{\text{dia}} + \chi_L, \tag{5}$$

which, along with the above-mentioned contributions, also includes the diamagnetism of conduction electrons χ_L . A rigorous calculation of χ_L is a rather difficult problem for a complicated band structure (see, e.g., Ref. 22), and the freeelectron Landau limit is often used for estimations, though for many systems this crude approximation has been found not to provide even the correct order of magnitude of the diamagnetic susceptibility. In fact, the agreement of the contributions to the magnetic susceptibility $\chi_{sum} = \bar{\chi}_{spin} + \bar{\chi}_{orb}$ $+ \chi_{dia}$ calculated here (see Table II) with the experimental value of χ (Table I) gives evidence that for CrB₂ the diamagnetic contribution χ_L is presumably negligible as compared with the dominant spin contribution χ_{spin} . In order to analyse the experimental data on the pressure effect in the magnetic susceptibility, the volume dependences of the paramagnetic contributions to susceptibility χ_{spin} and χ_{orb} are calculated *ab initio* within the field-induced FP-LMTO technique. The evaluated volume derivative $d \ln(\chi_{spin}+\chi_{orb})/d \ln V=4.0$ is in agreement with the experimental result for the PM phase of CrB₂, $d \ln \chi/d \ln V = 3.8 \pm 0.5$ (see Table I). It should be pointed out that the calculated value of the pressure effect on χ is predominately determined by the enhanced spin contribution χ_{spin} .

The measured pressure derivative of the magnetic susceptibility $d \ln \chi/dP$ can be used to derive the spontaneous volume change in CrB₂ due to the antiferromagnetic ordering $\Delta V/V \equiv \omega_m$, which is related to the squared local magnetic moment M(T) as²³

$$\omega_m(T) = \frac{C}{B} M^2(T).$$
(6)

Here *B* is the bulk modulus, and *C* is the magnetoelastic coupling constant. The latter can be determined within the phenomenological relation²⁴

$$\frac{C}{B} = -\frac{1}{2\chi V_m} \frac{d\ln\chi}{dP},\tag{7}$$

where χ and V_m are the molar susceptibility and volume, respectively. By using in Eq. (7) the experimental values of χ and $d \ln \chi/dP$ from Table I and $V_m = 14.1 \text{ cm}^3$, one estimates the magnetoelastic constant to be temperature independent within experimental errors and equal to $C/B = (1.07 \pm 0.15) \times 10^{-10} \text{ (e.m.u./mol)}^{-2}$. The substitution of the evaluated C/B value and the experimental magnetic moment $M(0) \approx 0.5 \mu_B/\text{Cr}$ (Ref. 5) in Eq. (6) yields the volume change at the AFM transition to be $\omega_m(0) \approx (0.083 \pm 0.012)\%$. This estimate agrees closely with the experimental value $\omega_m(0) = 0.085\%$.²⁵

The pressure dependence of the Néel temperature can be examined in line with a phenomenological approach of Ref. 26, which has been applied to the AFM chromium:

$$T_N \simeq \exp(-1/\lambda),\tag{8}$$

where kT_B is of the order of the *d*-band width, and $\lambda \propto IN(E_F)$. The volume dependence of the Stoner product $IN(E_F)$ can be obtained according to Eq. (2), which gives

$$\frac{d\ln\chi}{d\ln V} = \frac{d\ln N(E_F)}{d\ln V} + (S-1)\frac{d\ln[IN(E_F)]}{d\ln V}.$$
(9)

By substituting the experimental data on $d \ln \chi/d \ln V$ from Table I into Eq. (9) together with our estimates $d \ln N(E_F)/d \ln V = 1.52$ and $S \approx 8$, we obtain

$$\frac{d\ln[IN(E_F)]}{d\ln V} \simeq 0.3,\tag{10}$$

which means a substantial cancellation of the volume effects on the density of states at the Fermi level and the exchange parameter in the Stoner product $IN(E_F)$ of CrB_2 . Therefore, according to Eq. (8), the effect of pressure on T_N is mainly determined by the band-width behavior, $d \ln T_N/dP \approx d \ln T_B/dP$, and appears to be rather small and positive in sign. This is consistent with the measured weak pressure dependence of the Néel temperature in CrB_2 $(dT_N/dP = 0.1 \pm 0.1 \text{ K/kbar})$. It should be noted that such behavior of T_N differs essentially from that for pure chromium, where the strong suppression of the AFM state under pressure, with $dT_N/dP \approx -5.1 \text{ K/kbar}$ has been reported.²⁶ Therefore we can presume that a different mechanism of the magnetic ordering takes place in CrB_2 as compared to the AFM chromium.

To shed more light on the nature of the magnetic ordering in CrB₂, the electronic structure calculations for its lowtemperature helical magnetic structure are required. Such calculations are extremely difficult to perform, and in the present work the spin-polarized electronic structure calculations are carried out for the ferromagnetic phase of CrB₂. These calculations gave a spontaneous magnetic moment of $0.8\mu_B$, in reasonable agreement with experiment.⁵

V. CONCLUSIONS

For the first time the pressure effect on the magnetic susceptibility of CrB_2 is measured at temperatures both above and below T_N =87 K and is found to be almost independent of the magnetic state of the sample. Based on the obtained pressure derivative of the magnetic susceptibility, we evaluated the magnetoelastic coupling constant, which appears to describe correctly the reported spontaneous volume change in CrB₂ due to the antiferromagnetic ordering. The measured pressure effect on the Néel temperature is found to be considerably smaller than that for the pure AFM chromium, and this indicates that different mechanisms govern magnetic ordering in CrB₂ and Cr.

It is found that the Stoner approach underestimates substantially the spin susceptibility for the PM phase of CrB₂. This is presumably related to the deficiency of the Stoner approach wherein both parameters involved in the susceptibility enhancement, $N(E_F)$ and *I*, are calculated and averaged over the band states separately. It should be noted that a response function such as χ is microscopically nonuniform in space, and the induced magnetization density varies considerably within the unit cell. On the other hand, our *ab initio* calculations in an external magnetic field have yielded the main contributions to the magnetic susceptibility of CrB₂ and allowed us to describe the large value of χ and the magnetovolume effect $d \ln \chi/d \ln V$, in agreement with the experiment.

The authors thank Prof. I. V. Svechkarev and Dr. A. Grechnev for fruitful discussions and comments. This work has been supported by the Russian-Ukrainian RFBR-NASU project 8-2009.

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